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Rule Dependencies in Access Control Lists

Vic Grout  
*Glyndwr University, v.grout@glyndwr.ac.uk*

John McGinn  
*Glyndwr University, j.mcginn@glyndwr.ac.uk*

John N. Davies  
*Glyndwr University, j.n.davies@glyndwr.ac.uk*

Rich Picking  
*Glyndwr University, Wrexham, r.picking@glyndwr.ac.uk*

Stuart Cunningham  
*Glyndwr University, s.cunningham@glyndwr.ac.uk*

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Abstract
This paper considers the effects of dependencies between rules in Access Control Lists (ACLs). Dependent rules may not be reordered in an ACL if the policies of the list are to be preserved. This is an obstacle to the optimisation of rule order intended to reduce the time taken matching packets against rules. In this paper, the concept of rule dependency is defined in relation to the problem of minimising processing latency. The concepts of dependence and possible dependence are introduced and the relationship between them considered. Two measures of dependency, the dependency index and the fragmented dependency index are defined and formulated and an upper bound for each is derived. Examples of real-world ACLs are studied and the implications for practical optimisation discussed.

Keywords
access control lists (ACLs), rule dependencies, optimisation, packet latency

Disciplines
Computer and Systems Architecture | Digital Communications and Networking | Hardware Systems | Systems and Communications

Comments
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RULE DEPENDENCIES IN ACCESS CONTROL LISTS

Vic Grout, John McGinn, John Davies, Rich Picking and Stuart Cunningham
Centre for Applied Internet Research (CAIR), University of Wales, NEWI
Plas Coch Campus, Mold Road, Wrexham, LL11 2AW, UK
{v.grout|j.mcginn|j.n.davies|r.picking|s.cunningham}@newi.ac.uk

ABSTRACT
This paper considers the effects of dependencies between rules in Access Control Lists (ACLs). Dependent rules may not be reordered in an ACL if the policies of the list are to be preserved. This is an obstacle to the optimisation of rule order intended to reduce the time taken matching packets against rules. In this paper, the concept of rule dependency is defined in relation to the problem of minimising processing latency. The concepts of dependence and possible dependence are introduced and the relationship between them considered. Two measures of dependency, the dependency index and the fragmented dependency index are defined and formulated and an upper bound for each is derived. Examples of real-world ACLs are studied and the implications for practical optimisation discussed.

KEYWORDS
Access Control Lists (ACLs), Rule dependencies, Optimisation, Packet latency.

1. INTRODUCTION: ACCESS CONTROL LISTS

Access Control Lists (ACLs) play a major rôle in the process of passing or blocking traffic through certain regions of a network. They can permit or deny traffic from or to given sources or destinations, or discriminate on the basis of content or other characteristics. In addition, their ability to filter network traffic makes ACLs suitable for a wider purpose; any in which there is a need to choose certain traffic, probably as data packets, for a given policy. Network Address Translation (NAT), traffic shaping, various aspects of Internet routing, and numerous other traffic policies all require packets to which the policy is to be applied to be separated from those to which it is not. ACLs may vary considerably in size, structure and purpose but it is not uncommon for each packet to be tested against several ACLs on its passage across a single internet router and many more across a complete autonomous system or domain. It is therefore useful to optimise ACLs for efficiency.

An ACL is an ordered list of rules. Each rule accepts or rejects a packet based on one or some of its characteristics - its profile. Typically, a packet may be considered on the basis of its source and/or destination address or traffic type, although other features, or flags, may be relevant (Cisco, 2000, Sedayao, 2001). Figure 1 gives an example of a typical ACL in the syntax of the Cisco Internetwork Operating System (IOS) (JANet, 2005). The use of the terms permit and deny reflect the original role of ACLs in passing or blocking traffic (although their use is now considerably more widespread). Each packet to be tested against an ACL is compared with the first rule, then the second, and so on, until a rule matches its profile. The rule is then permitted or denied accordingly and no more rules are considered. There is taken to be an implicit ‘deny all’ rule terminating each list to deal with packets not matched by any other rule. ACL optimisation effectively means finding an ordering of its rules that minimises processing time and thus packet latency.

However, rule order can be critical in an ACL. To illustrate this, consider two rules as follows: rule 1 permits packets with characteristic A (source address, for example) and rule 2 denies packets with characteristic B (destination address, say). A packet with a profile matching both characteristics (from A to B in this case) will match both rules. The rules are dependent. Consequently, the order of rule 1 ... rule 2 will permit the A to B packet whereas the order rule 2 ... rule 1 will deny it. In Figure 1, rules 8 and 9 are dependent: an SMTP packet from the 192.168.2.0 network to the mail-server will match both rules. It is the intention of the policy, in its given form, that such a packet should be blocked. However, promoting rule 9
above rule 8 would (incorrectly) pass it. Not all rules will be dependent in this way but those that are must have their relative order in the list preserved if the ACL is to retain its intended purpose. Of course, this only applies for rules of opposite types. Several ‘permit’ rules in a contiguous block, for example, can be freely reordered among themselves. This paper considers the effect of dependent rules on the effectiveness of any optimisation (latency minimisation) process.

(1) access-list 173 permit icmp any any
(2) access-list 173 permit tcp any any established
(3) access-list 173 deny ip RANGE MASK any
(4) access-list 173 deny ip 10.77.23.0 0.255.255.255 any
(5) access-list 173 deny ip 172.16.2.0 0.15.255.255 any
(6) access-list 173 deny ip 192.168.1.0 0.0.255.255 any
(7) access-list 173 deny ip 169.254.1.0 0.0.255.255 any
*(8) access-list 173 deny ip 192.168.2.0 0.0.0.255 any
*(9) access-list 173 permit tcp any host MAILSERVER eq smtp
(10) access-list 173 permit tcp any host NAMESERVER eq domain
(11) access-list 173 permit udp any host NAMESERVER eq domain
(12) access-list 173 permit udp any eq 53 host NAMESERVER gt 1024
(13) access-list 173 permit tcp host MANAGER host SUN eq telnet
(14) access-list 173 permit tcp host MANAGER host SERIAL0 eq telnet
(15) access-list 173 permit udp host MANAGER host SERIAL0 eq smtp
(16) access-list 173 permit tcp host MANAGER host ETHERNET0 eq telnet
(17) access-list 173 permit tcp host MANAGER host SUN eq telnet
(18) access-list 173 permit tcp any eq 53 host NAMESERVER gt 1024
(19) access-list 173 permit tcp any eq 53 host NAMESERVER gt 1024
(20) access-list 173 permit tcp any host NMSERVER eq www
(21) access-list 173 permit tcp any host NMSERVER eq port 80
(22) access-list 173 permit udp EXT-NTPSERVER any eq 123
(23) access-list 173 permit udp any range 6970 7170 any
(24) access-list 173 deny ip any any

Figure 1. An Example of an Access Control List (ACL).

2. ACL OPTIMISATION AND RULE DEPENDENCIES

Where appropriate in this paper, abbreviations are used as follows: \( \exists \) ‘there is’ or ‘there exists’; \( \forall \) ‘for all’ or ‘for every’; \( \land \) ‘and’; \( \Leftrightarrow \) ‘if and only if’; and \( \rightarrow \) ‘such that’. Using the notation of Grout and McGinn (2005), define \( A^* \) to be the set of all addresses available within a given system, define \( B^* \) to be the set of all protocols recognised by the system and define \( F^* = \{0, 1\}^* \) to be the set of w flag vectors \( \langle 0, 1 \rangle \) w-tuples acting on \( B^* \) valid for the system. For completeness only, \( X^* \) represents the set of payloads.

A packet, \( p_i = (s_{i0}, d_{i0}, b_{i0}, f_i, X_i) \), is defined by its constituents: \( s_{i0} \in A^* \), the source address; \( d_{i0} \in A^* \), the destination address; \( b_{i0} \in B^* \), the protocol; \( f_i \in F^* \), the flags vector and \( X_i \in X^* \), the payload. A rule, \( r_i = (t_i, s_{i0}, d_{i0}, b_{i0}, f_i) \), consists of: a type, \( t_i \in \{\text{permit, deny}\} \), \( s_{i0} \in A^* \), the source range, \( d_{i0} \in A^* \), the destination range, \( b_{i0} \in B^* \), the protocol range, and a flags predicate, \( \sigma: F^* \rightarrow \{\text{true, false}\} \). Only \( t_i \) is a required component in all syntaxes. If any other components are absent then \( s_{i0} = A^* \), \( d_{i0} = A^* \), \( b_{i0} = B^* \) or \( \sigma = \text{true by default.} \) A policy, \( Z = r_1, r_2, ..., r_n \) is an (ordered) sequence of n rules to achieve some purpose. The last rule in any policy implicitly denies all traffic; that is, \( t_n = \text{deny} \), \( s_{n0} = A^* \), \( d_{n0} = A^* \), \( b_{n0} = B^* \) and \( \sigma_n = \text{true.} \) A packet, \( p_k \), matches a rule, \( r_i \) (for which we write \( p_k \triangleright r_i \)), if its addresses and protocols are within the range of the rule and if its flags vector satisfies the rule’s flags predicate. That is,

\[
p_k \triangleright r_i \iff (s_{ik} \in SA_i) \land (d_{ik} \in DA_i) \land (b_{ik} \in Bi) \land \sigma(f_i).
\]

in which case the packet will be permitted or denied according to \( t_i \).

A dependency exists between two rules, \( r_i \) and \( r_j \), if they are of opposite type and it is possible that there exists a packet, \( p_k \), that matches both rules \((p_k \triangleright r_i) \land (p_k \triangleright r_j)\); that is \( r_i \) and \( r_j \) are dependent if

\[
(t_i \neq t_j) \land \exists p_k \rightarrow (s_{ik} \in SA_i \cap SA_j) \land (d_{ik} \in DA_i \cap DA_j) \land (b_{ik} \in Bi \cap Bj) \land \sigma(f_i) \land \sigma(f_j).
\]
Eliminating the packet, \( p \), from this expression, allows a \([0, 1]\) dependency matrix, \( D = (d_{ij}: 1 \leq i, j \leq n) \), to be defined:

\[
d_{ij} \Leftrightarrow (t_i \neq t_j) \land (SA_i \cap SA_j \neq \emptyset) \land (DA_i \cap DA_j \neq \emptyset) \land (B_i \cap B_j \neq \emptyset) \land (\Sigma_i \cap \Sigma_j \neq \emptyset),
\]

where \( \Sigma \subseteq F^* \) is the subset of flag vectors satisfying \( \sigma \). Two rules, \( r_i \) and \( r_j \), are possibly dependent if they are of opposite type \( (t_i \neq t_j) \), giving a possible dependency matrix, \( P = (p_{ij}: 1 \leq i, j \leq n) \), defined as \( p_{ij} \Leftrightarrow (t_i \neq t_j) \). If \( d_{ij} = 1 \) then the order of rules \( i \) and \( j \) must be preserved if the behaviour of the policy is to be maintained. Detecting dependencies and anomalies, particularly in real-time on a production router is not trivial, however (Hari et al., 2000, Al-Shaer and Hamed, 2004). If there is any uncertainty then it may be necessary to apply the same restriction when \( p_{ij} = 1 \).

An access list, or simply list, \( L \), implements a policy, \( Z = [r_1, r_2, ..., r_n] \), if it is a permutation of the rules of \( Z \) such that the order of dependencies is preserved. Let \( r_i(L) \) be the rule at position \( i \) in \( L \). A special case of a list implementing a policy, \( Z \), is the identity list, \( I_Z = [r_1, r_2, ..., r_n] \), for which \( r_i(I_Z) = r_i \forall i (1 \leq i \leq n) \). \( I_Z \) is usually the starting point for any ACL optimisation, particularly iterative search techniques.

The hit-rate, \( h(r_i(L)) \), of rule \( r_i \) in a list \( L \), is the probability that a packet will match \( r_i \) in \( L \). Hit-rates can be calculated dynamically using counters within the IOS or hardware (Cisco, 2002 & 2003). The latency, \( \lambda(r_i) \), of a rule \( r_i \) is the time taken to (independently) process \( r_i \). This may be calculated from the length of a rule, the nature of the protocols involved or taken from stored tables. In some systems, latencies may be constant for all rules but this is not assumed in this paper. The cumulative latency, \( \kappa(r_i(L)) \), of \( r_i \) in a list \( L \), is the time taken to process \( r_i \) and all rules preceding it in \( L \).

\[
\kappa(r_i(L)) = \sum_{\varphi=1}^{i} \lambda(r_{\varphi}(L)).
\]

The expected latency, \( E(L) \), of a list \( L \), is then given by

\[
E(L) = \sum_{i=1}^{n} h(r_i(L))\kappa(r_i(L)) = \sum_{i=1}^{n} h(r_i(L))\sum_{\varphi=1}^{i} \lambda(r_{\varphi}(L)).
\]

Optimising an ACL requires us to find (or approximate) the list, \( L \), implementing a policy, \( Z \), that minimises \( E(L) \), subject to the constraints of the dependency matrices, \( D \) or \( P \). Grout and McGinn (2005) show the problem to be \( NP\text{-}complete \) (Garey and Johnson, 1979).

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<td>22</td>
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<td>X</td>
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</table>

Figure 2. Rule Dependencies.
3. DEPENDENCY INDICES AND BOUNDS

Define the *dependency index* (DI) to be the ratio of dependent rule pairs to all rule pairs. Larger numbers of rule dependencies (larger DIs) restrict ACL optimisation by making more potential rule reorderings (e.g., swaps) illegal (Grout et al., 2006). For *n* rules, there are *n*<sup>2</sup> potential dependencies. However, dependencies are not possible between rules of the same type so, for a policy of *x* permits and *y* denys (*n = x + y*), the number of possible dependencies is *n*<sup>2</sup> − *x*<sup>2</sup> − *y*<sup>2</sup> with DI bounded above by (*n*<sup>2</sup> − *x*<sup>2</sup> − *y*<sup>2</sup>)/*n*<sup>2</sup>. Figure 2 shows these relationships for the ACL in Figure 1 with *n* = 24, *x* = 17, *y* = 7 and DI ≤ (576 − 289 - 49)/576 = 0.41. Figure 3 shows how the limit for DI varies with *x* (and *y*), the minimum value of 0 occurring when *x* (or *y*) = *n* and the maximum value of 0.5 when *x* = *y* = *n*/2.

*Figure 3. A Bound for the Dependency Index (DI).*

DI provides a measure of the (lack of) freedom to reorder rules in the optimisation process. However, this assumes that all rule swaps (say) are considered within the optimisation algorithm (Bukhatwa and Patel, 2003, Bukhatwa, 2004, Grout and McGinn, 2005, for example). In the real-world, such an approach would be too complex to be embedded in a router’s hardware or software and, typically, only adjacent swaps are considered (Grout et al., 2005). If the search algorithm prohibits swaps between non-adjacent (permit or deny) blocks then a different dependency index is required to be meaningful.

To this end, suppose an ACL, *L*, consists of *b*<sub>x</sub> blocks of permits, *X*<sub>j</sub> (1 ≤ *j* ≤ *b*<sub>x</sub>) and *b*<sub>y</sub> blocks of denys, *Y*<sub>k</sub> (1 ≤ *k* ≤ *b*<sub>y</sub>). Then

\[
n = x + y = \sum_{j=1}^{b_x} |X_j| + \sum_{k=1}^{b_y} |Y_k|, \tag{6}
\]

where |*B*| represents the number of rules in block *B*. If swaps are not permitted (or considered) between non-contiguous blocks, then the number of infeasible or possibly dependent pairs is increased to

\[
n^2 - \sum_{j=1}^{b_x} |X_j|^2 - \sum_{k=1}^{b_y} |Y_k|^2 \tag{7}
\]

(again consider Figure 2) and the fragmental dependency index (FDI) bounded above by...
\[
\frac{1}{n^2} \left( n^2 - \sum_{j=1}^{b_x} X_j^2 - \sum_{k=1}^{b_y} Y_k^2 \right).
\]

(8)

For the example in Figures 1 and 2, \( b_x = b_y = 2, |X_1| = 2, |Y_1| = 6, |X_2| = 15 \) and \( |Y_2| = 1 \) giving \( \text{FDI} \leq \frac{(576 - 4 - 36 - 225 - 1)}{576} = 0.54 \). In general, FDI is minimised when \( b_x = 1 \) and \( b_y = 0 \) (\( |X_1| = n \)) or \( b_x = 0 \) and \( b_y = 1 \) (\( |Y_1| = n \)) and maximised by alternating single permits and denys \( (b_x = b_y = n/2, |X_j| = |Y_k| = 1 \ \forall \ 1 \leq j,k \leq b_x,b_y) \) giving a bound of \( (n^2 - n) / n^2 \), which tends to 1 as \( n \) increases – the worst case. Figure 4 illustrates the general bound for equally sized permit/deny blocks, \( |X_j| = |Y_k| = n / (b_x + b_y) \) \( \forall \ 1 \leq j \leq b_x \) and \( 1 \leq k \leq b_y \).

![Figure 4. Typical Bound for the Fragmented Dependency Index (FDI).](image)

4. ANALYSIS AND RESULTS

This section uses the DI and FDI of real-world ACLs to discuss the suitability of simple optimisation techniques. Grout et al. (2006) propose the following three-part heuristic, called \( \delta\text{-OPT} \), for simple, embedded minimisation of expected latency:

**Step 1:** Initialisation (following manual ACL configuration)

For \( i := 1 \) to \( n \) do

\[
h_i := 1 \quad \text{\( \backslash \) hit rates equal at start}
\]

**Step 2:** Promotion (on a packet matching rule \( i \))

\[
h(r_i) := 2h(r_i) \quad \text{\( \backslash \) exponentially increase matched hit-rate}
\]

if \( (d_{i-1} = 0) \) and \( (h(r_i) \lambda(r_{i-1}) > h(r_{i-1}) \lambda(r_i)) \) then \( \text{\( \backslash \) (or } p_{i-1} = 0) \)

\[
\text{Swap}(r_{i-1}, r_i) \quad \text{\( \backslash \) promote if } E(L) \text{ reduced}
\]

**Step 3:** Reduction (periodically to prevent overflow)

For \( i := 1 \) to \( n \) do

\[
h(r_i) := h(r_i) / \max_j h(r_j)
\]

Derivation and details are to be found in the original paper. There is some processing cost associated with implementing this algorithm. However, depending upon the nature of the traffic and dependency indices of the rules, this simple optimisation can be shown to be worthwhile (i.e. to reduce overall expected latency) for ACLs above a certain length (number of rules, \( n \)). Table 1 summarises these results as the minimum number
of rules for the saving in ACL latency to outweigh the latency from the algorithm. $S$ is the stability of the traffic flow, essentially a probability that a given packet is similar to the previous one in that it matches the same rule in the ACL, $L$. $\delta$-OPT performs better for more stable traffic. However, only for values of DI approaching 1 is optimisation worthless.

Table 1. Minimum value of $n$ for $\delta$-OPT to reduce $E(L)$

<table>
<thead>
<tr>
<th>$S$</th>
<th>0.00</th>
<th>0.25</th>
<th>0.50</th>
<th>0.75</th>
<th>1.00</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.00</td>
<td>19</td>
<td>21</td>
<td>23</td>
<td>33</td>
<td>$\infty$</td>
</tr>
<tr>
<td>0.25</td>
<td>16</td>
<td>19</td>
<td>21</td>
<td>29</td>
<td>$\infty$</td>
</tr>
<tr>
<td>0.50</td>
<td>13</td>
<td>15</td>
<td>19</td>
<td>26</td>
<td>$\infty$</td>
</tr>
<tr>
<td>0.75</td>
<td>9</td>
<td>10</td>
<td>13</td>
<td>21</td>
<td>$\infty$</td>
</tr>
<tr>
<td>1.00</td>
<td>8</td>
<td>9</td>
<td>12</td>
<td>17</td>
<td>$\infty$</td>
</tr>
</tbody>
</table>

As an example, on the basis of these results and the calculations from Section 3, $\delta$-OPT can be seen to have a positive benefit for the ACL in Figure 1 for all traffic flows, $S$. (DI = 0.41 and FDI = 0.54, $n = 24$ and, from Table 1, taking an index of 0.5, optimisation will be worthwhile for ACLs larger than 23 rules, even for the worst case, $S = 0$.) This analysis is now applied to a number of real-world ACLs. Table 2 summarises the characteristics of several ACLs taken from a variety of production applications. (No attempt has been made to remove redundancies/inconsistencies, etc. from these ACLs: they are taken directly from source.) ACLs B, C and D are taken from college/university LANs, F, G and H from company networks and A and E from SOHO environments connecting to the Internet via an ISP. ACLs I, J and K are derived from templates for various standard security configurations. In each case, the upper bound is calculated for the two dependency indices. These values are plotted in Figure 5 for comparison.

Table 2. Permit/deny block structure for various real-world ACLs with corresponding dependency indices

<table>
<thead>
<tr>
<th>ACL</th>
<th>$n$</th>
<th>$x$</th>
<th>$y$</th>
<th>$b_x$</th>
<th>$b_y$</th>
<th>$X_i$</th>
<th>$Y_k$</th>
<th>DI*</th>
<th>FDI*</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>16</td>
<td>10</td>
<td>6</td>
<td>2</td>
<td>3</td>
<td>6, 4</td>
<td>2, 3, 1</td>
<td>0.47</td>
<td>0.74</td>
</tr>
<tr>
<td>B</td>
<td>55</td>
<td>20</td>
<td>33</td>
<td>4</td>
<td>4</td>
<td>10, 7, 2, 1</td>
<td>14, 12, 5, 2</td>
<td>0.47</td>
<td>0.81</td>
</tr>
<tr>
<td>C</td>
<td>55</td>
<td>10</td>
<td>45</td>
<td>2</td>
<td>3</td>
<td>5, 5</td>
<td>27, 17, 1</td>
<td>0.30</td>
<td>0.65</td>
</tr>
<tr>
<td>D</td>
<td>144</td>
<td>27</td>
<td>117</td>
<td>6</td>
<td>7</td>
<td>4, 7, 6, 6, 3, 1</td>
<td>18, 32, 12, 6, 25, 21, 3</td>
<td>0.30</td>
<td>0.87</td>
</tr>
<tr>
<td>E</td>
<td>19</td>
<td>7</td>
<td>12</td>
<td>1</td>
<td>2</td>
<td>7</td>
<td>6, 6</td>
<td>0.47</td>
<td>0.66</td>
</tr>
<tr>
<td>F</td>
<td>93</td>
<td>22</td>
<td>71</td>
<td>3</td>
<td>4</td>
<td>13, 8, 1</td>
<td>41, 17, 12, 1</td>
<td>0.36</td>
<td>0.73</td>
</tr>
<tr>
<td>G</td>
<td>111</td>
<td>29</td>
<td>82</td>
<td>1</td>
<td>2</td>
<td>29</td>
<td>80, 2</td>
<td>0.39</td>
<td>0.41</td>
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<tr>
<td>H</td>
<td>62</td>
<td>4</td>
<td>58</td>
<td>2</td>
<td>3</td>
<td>2, 2</td>
<td>22, 32, 4</td>
<td>0.12</td>
<td>0.60</td>
</tr>
<tr>
<td>I</td>
<td>172</td>
<td>54</td>
<td>118</td>
<td>2</td>
<td>3</td>
<td>31, 23</td>
<td>77, 40, 1</td>
<td>0.43</td>
<td>0.70</td>
</tr>
<tr>
<td>J</td>
<td>68</td>
<td>19</td>
<td>49</td>
<td>4</td>
<td>5</td>
<td>1, 1, 15, 2</td>
<td>16, 8, 12, 10, 3</td>
<td>0.40</td>
<td>0.83</td>
</tr>
<tr>
<td>K</td>
<td>63</td>
<td>22</td>
<td>41</td>
<td>2</td>
<td>3</td>
<td>18, 14</td>
<td>18, 13, 10</td>
<td>0.45</td>
<td>0.76</td>
</tr>
</tbody>
</table>

* upper bound

On the basis of the derived dependency indices in Table 2, and the limits given in Table 1, Table 3 summarises the effectiveness of the $\delta$-OPT heuristic for each of the ACLs, A, B, ..., K. In each case, and separately for each of DI and FDI, the algorithm is marked as worthwhile or otherwise depending on whether its cost in terms of implementation is exceeded by the gain in expected latency.

Table 3 suggests that, at least for the ACLs tested, the choice of DI or FDI bound for assessing the viability of the $\delta$-OPT algorithm for different lists may not be as important as might be thought. Only in 3 of the 55 ACL/traffic combinations does it affect the effectiveness of the algorithm. Whether or not this is true
generally does not affect this paper’s outcomes. The point is that these bounds can be used in this manner to assess algorithmic performance.

![Figure 5](image)

**Figure 5.** Comparing Bounds for DI and FDI for real-world ACLs.

**Table 3.** Effectiveness of $\delta\text{-OPT}$ for real-world ACLs

<table>
<thead>
<tr>
<th>ACL</th>
<th>$S =$</th>
<th>0.00</th>
<th>0.25</th>
<th>0.50</th>
<th>0.75</th>
<th>1.00</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>DI* / FDI*</td>
<td>0 / 0</td>
<td>0 / 0</td>
<td>0 / 0</td>
<td>0 / 0</td>
<td>0 / 0</td>
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<tr>
<td>B</td>
<td>1 / 0</td>
<td>1 / 0</td>
<td>1 / 1</td>
<td>1 / 1</td>
<td>1 / 1</td>
<td></td>
</tr>
<tr>
<td>C</td>
<td>1 / 1</td>
<td>1 / 1</td>
<td>1 / 1</td>
<td>1 / 1</td>
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<td></td>
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<tr>
<td>D</td>
<td>1 / 1</td>
<td>1 / 1</td>
<td>1 / 1</td>
<td>1 / 1</td>
<td>1 / 1</td>
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<td>1 / 0</td>
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<tr>
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<td>1 / 1</td>
<td>1 / 1</td>
<td>1 / 1</td>
<td>1 / 1</td>
<td></td>
</tr>
<tr>
<td>K</td>
<td>1 / 1</td>
<td>1 / 1</td>
<td>1 / 1</td>
<td>1 / 1</td>
<td>1 / 1</td>
<td></td>
</tr>
</tbody>
</table>

* 1: worthwhile 0: not worthwhile

**5. CONCLUSIONS**

We deal initially with the limitations of this work. Firstly, no attempt has been made to tighten the (upper) bounds on DI and FDI. It is unlikely to be possible to achieve this formally and to compare rules in a pairwise manner is far from trivial individually and is extremely complex for an entire ACL (Hari et al., 2000, Al-Shaer and Hamed, 2004). An empirical study of the relationship between actual DI and FDI values and their theoretical bounds for real-world ACLs is beyond a paper of this length but is left open as an avenue for future research. Secondly, comparative results are only given for the $\delta\text{-OPT}$ heuristic. This is partly because this is the only ACL optimisation process sufficiently efficient to be embedded in router hardware (Grout et al., 2006) and partly because only for $\delta\text{-OPT}$ are the limit values in Table 1 available. However, extending the analysis to other forms of optimisation (Cisco, 2002, 2003 & 2004, Bukhatwa and
Patel, 2003, Bukhatwa, 2005, Grout and McGinn, 2005, for example), whilst not providing efficient solutions, may serve to aid the analysis of the relationship between DI and FDI and their bounds and their different behaviour for ACLs with varying (e.g. block) structures. Thirdly, while the significance of different traffic characteristics is recognised (by the stability factor, $S$), this cannot be pursued to the fullest extent here.

There are a number of satisfactory outcomes, however. Firstly, the matching of packets and rules and the optimisation of rule order within ACLs is formalised to enable the relationship between ACL structure and rule dependency to be analysed. The optimisation objectives of minimising expected latency are hindered by excessive dependence between rules and may render certain ACLs, or types of ACLs inappropriate for optimisation. This can be measured, in principle, by the DI and FDI dependency indices and, in practice, approximated by their bounds. A simple formula is given for each bound that can be calculated easily for any ACL. A number of tests on real world ACLs then demonstrate how these bounds, in conjunction with empirical testing and simulation (Grout et al., 2006), show how ACLs may be classified conveniently as appropriate or inappropriate for optimisation.

REFERENCES